



# Overview of Muon Collider Rings, MDI and Background Mitigation

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# Design Goals

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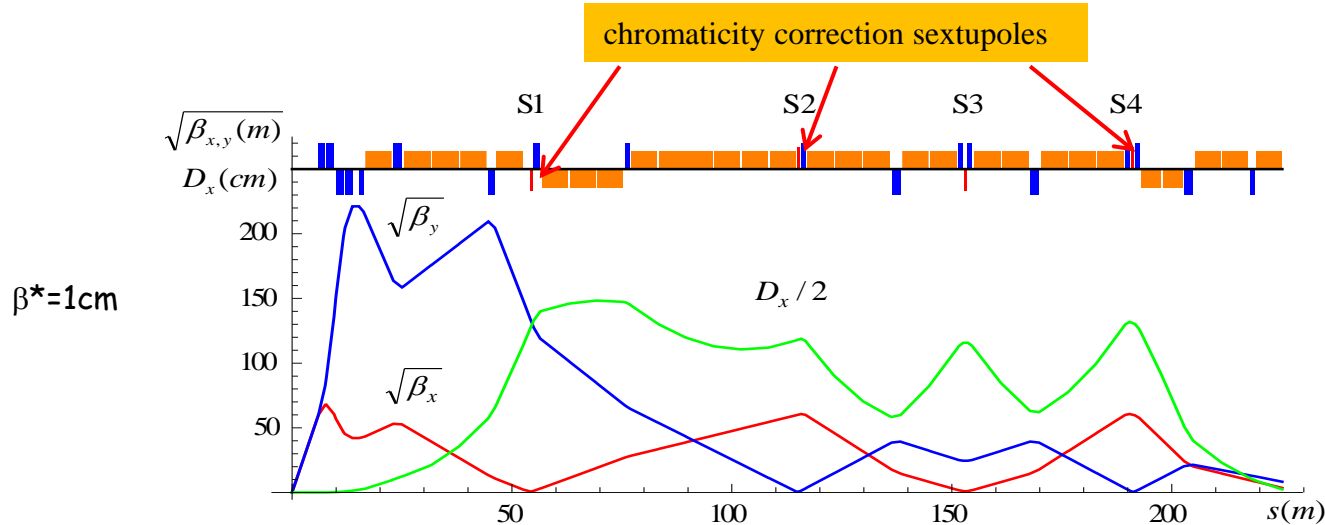
## Lattice design goals:

- High Luminosity (small  $\beta^*$ , circumference, momentum compaction)
- Acceptable detector backgrounds (tight apertures, dipole component in FF quads, halo suppression)
- Manageable heat loads in magnets (W absorbers and masks, shorter magnets, again dipole component in quads)
- $\beta^*$  variation in wide range (w/o breaking dispersion closure)
- Limited  $\beta_{\max}$  to reduce required apertures and sensitivity to errors.
- Higgs Factory: small collision energy spread  $\sigma_E/E \leq 4 \cdot 10^{-5}$
- High Energy MC ( $E_{\text{com}} \geq 3 \text{ TeV}$ ): safe levels of  $\nu$ -induced radiation (no long straights, combined-function magnets to spread  $\nu$ 's)

## Magnet design goals:

- High nominal fields in the required (large) aperture
- Sufficient operation margin to work at high dynamic heat load
- Accelerator beam quality in the beam area
- Not just theoretical feasibility, but also technological realizability (stress management, cooling, quench protection, protection from radiation, production process!)

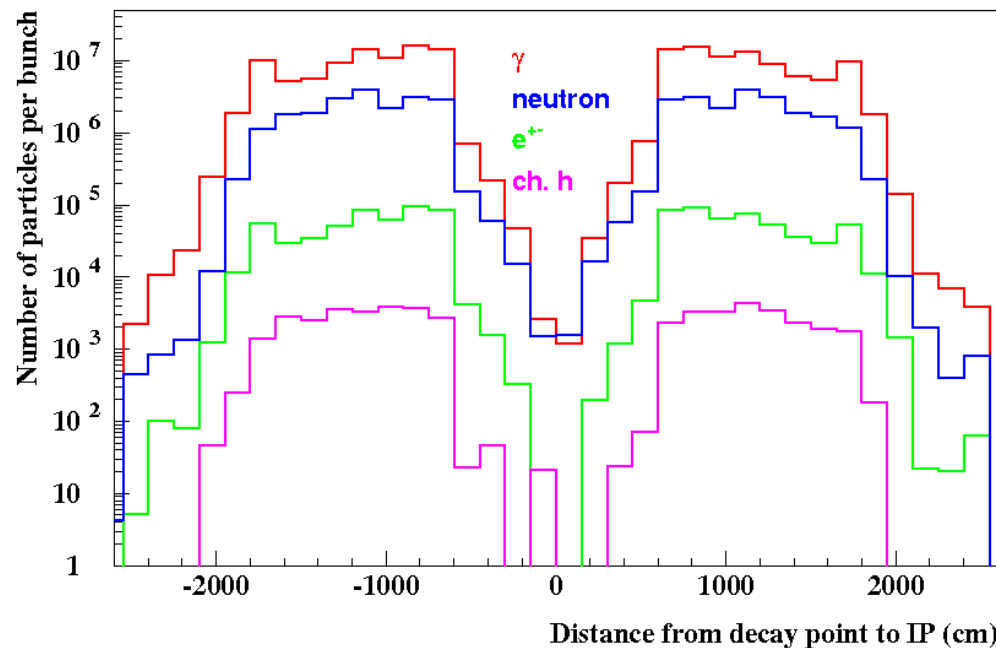
# $E_{\text{com}} = 1.5 \text{ TeV}$ Collider Lattice



This was chronologically the first successful design (November 2009) for which an (almost) full cycle of studies was completed:

- 3-sextupole chromaticity correction scheme developed  $\rightarrow$  stable momentum range  $\pm 1.2\%$ ,  $DA > 4\sigma$  w/o errors
- Magnet design for entire ring (10T pole tip field assumed)
- Heat deposition and detector background simulations  $\rightarrow$  important conclusions (see next slides), the background level achieved  $\sim$  that at LHC
- Study of systematic field errors (fringe fields and multipoles) and attempt to correct them (finished with  $DA \approx 3\sigma$  due to open-midplane magnet multipoles)
- Study of beam-beam effects (including strong-strong)

# Background Source Tagging for 1.5 TeV MC



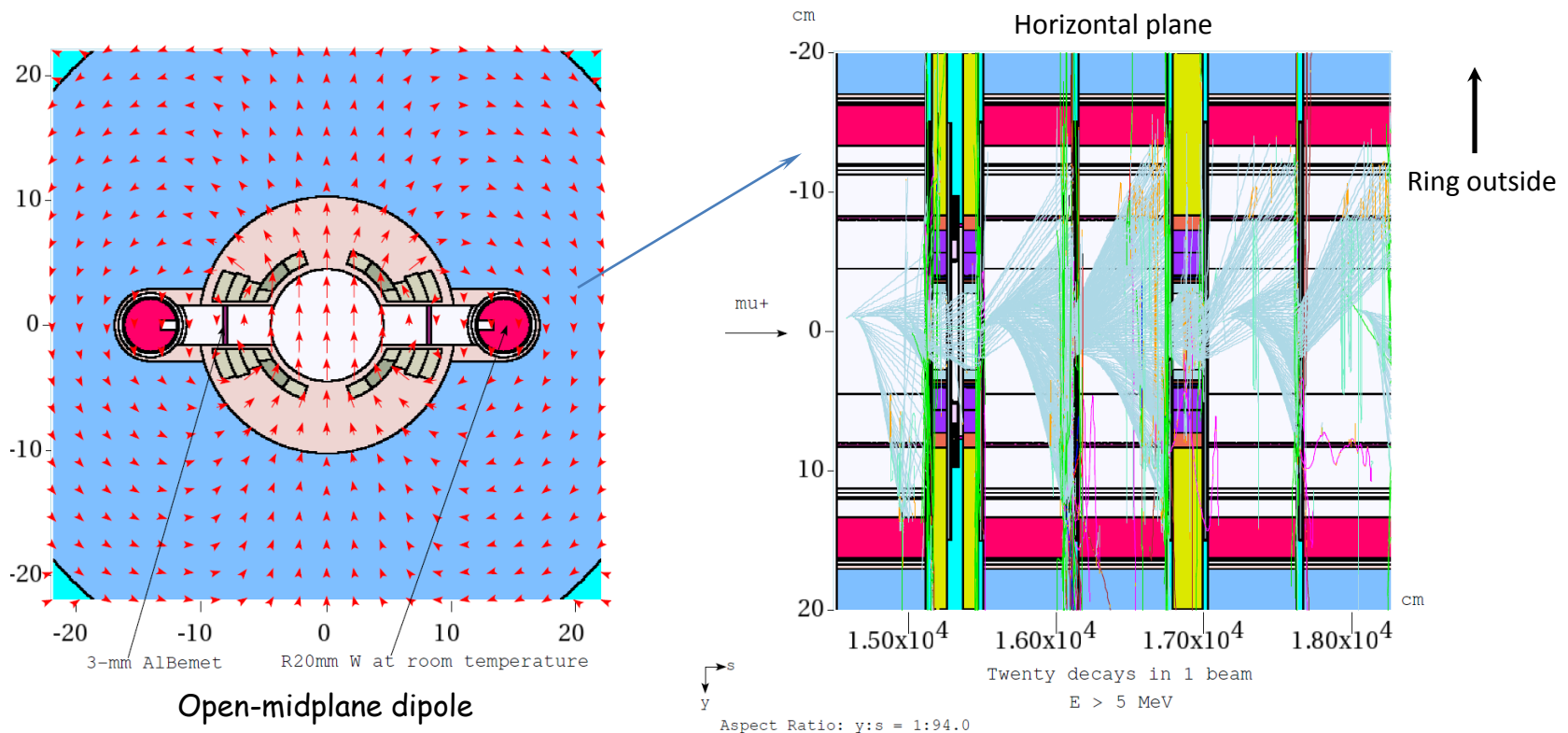
For BH muons the  
origin within  $\pm 100\text{m}$

All background species (except BH muons) originate from region  $\pm 18\text{m}$  w/o strong dipole field (though there is 2T in defocusing quads).

This result settles the discussion if a dipole field in the detector vicinity is a good or a bad thing - it is needed!

The subsequent designs for Higgs Factory and 3 TeV collider employed quadruplet Final Focus with 2T dipole field in the 2<sup>nd</sup> from IP quad (see support slides for detail)

# Showers from $\mu^+$ Decays in CC Section

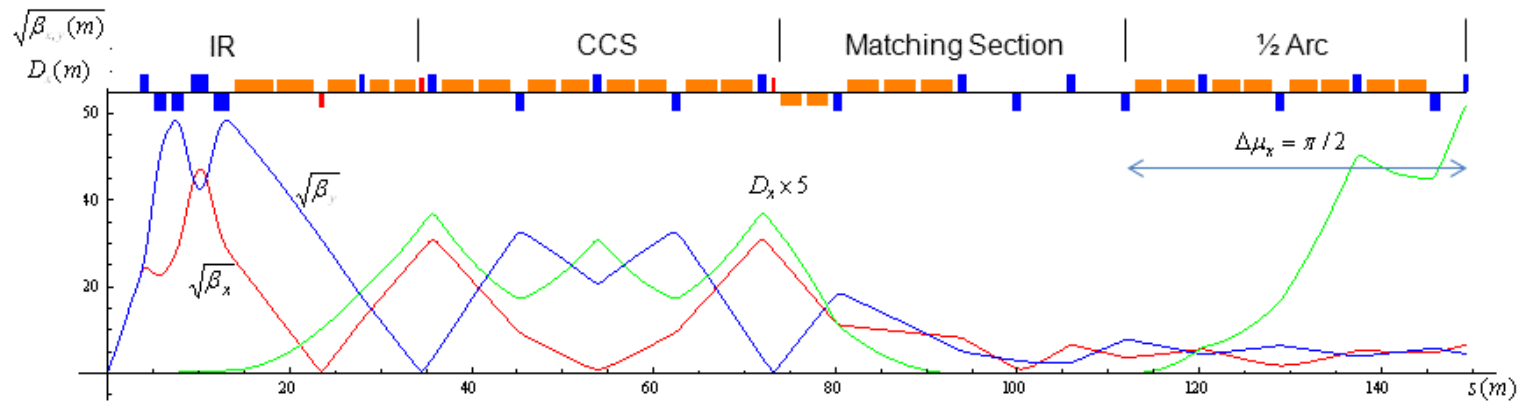


- Energy deposition in quads may exceed  $\text{Nb}_3\text{Sn}$  quench limit due to “punch through” the masks from midplane gaps in dipoles
- Decay electrons linger at field-reversal radial position in dipoles and eventually hit vertically the cold mass, not the rods
- Electrons are spread by quadrupoles  $\rightarrow$  synchrotron  $\gamma$ 's hit elements on the outside of dipoles

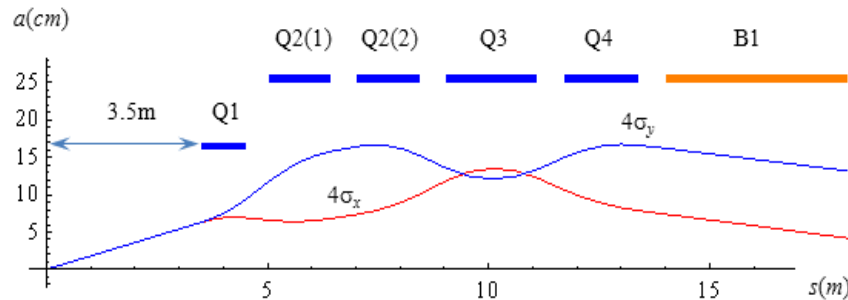
Open-midplane dipoles do not work

Combined-function magnets can be helpful

# Higgs Factory Lattice

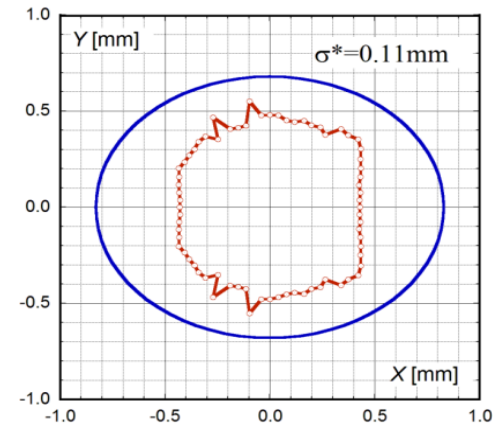


Higgs Factory lattice and optics functions for  $\beta^*=2.5\text{cm}$  in a half-ring starting from IP



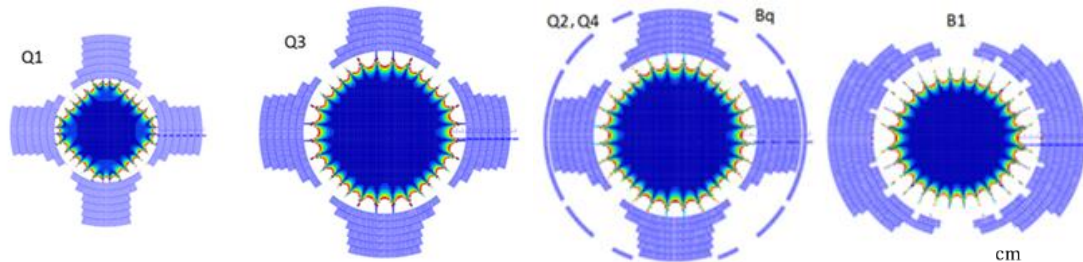
IR quad cold mass inner radii and  $4\sigma$  beam envelopes for  $\beta^*=2.5\text{cm}$ .  
Q2 and Q4 have 2T dipole component (need higher?)

**Very large magnet aperture required due to high transverse emittance  $\rightarrow$  fringe fields !**



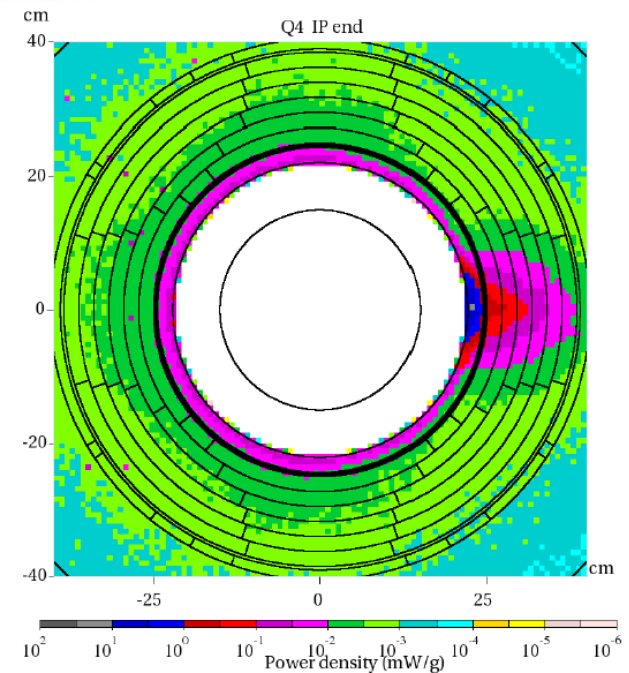
The dynamic aperture (fringe fields + multipoles + correction on) and projection of FF quad aperture (solid ellipse).

# Large Aperture Magnet Design



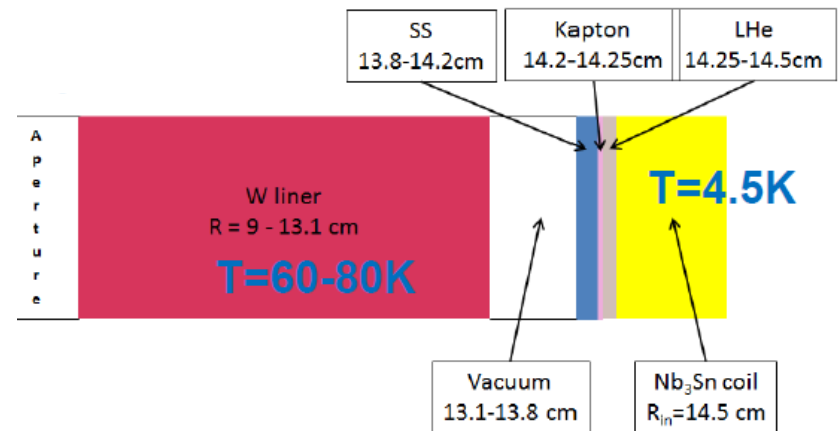
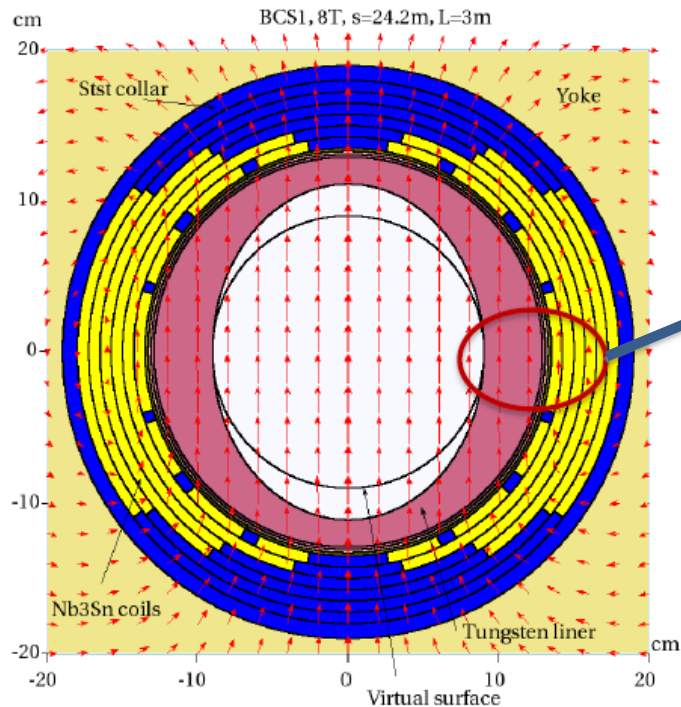
	Q1	Q2	Q3	Q4
aperture (cm)	32	50	50	50
gradient (T/m)	74	-36	44	-25
dipole field (T)	0	2	0	2
length (m)	1.0	1.4	2.05	1.7
$B_{\text{coil}}$ (T)	16.4	17.2	16.9	(17.2)
Margin @ 4.5°K	0.78	0.62	0.70	(0.62)

- 6-layer, shell-type coil design achieves the design goals with sufficient margin
- Good field quality region (deep blue)  $\sim 0.7$  of the aperture determines the DA

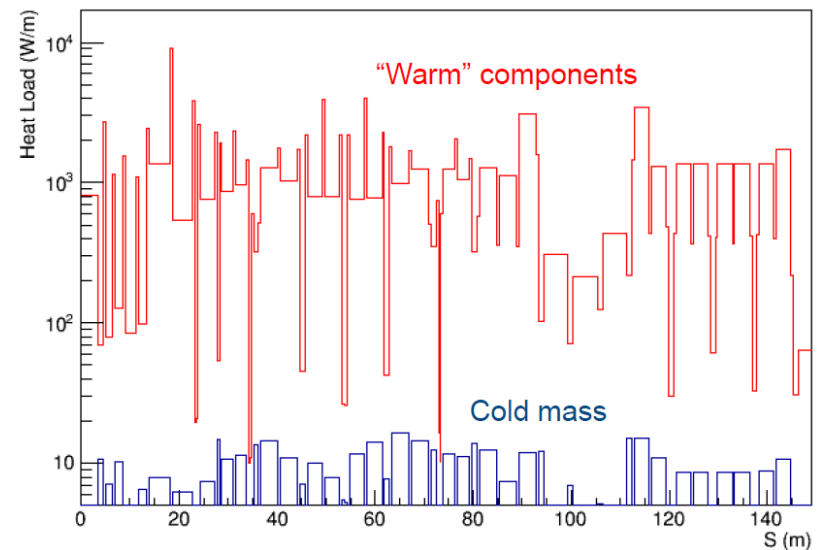


- Masks between the quads at  $4\sigma$  and inner absorbers reduced heat loads from 100-150mW/g to  $<1.5\text{mW/g}$

# Dynamic Heat Load



- Due to smaller circumference and higher muon flux the heat load in HF of  $\sim 1\text{ kW/m}$  is twice higher than in high-energy MC
- With W masks optimized individually for each magnet interconnect region and with elaborate inner absorbers (top) the cold mass heat load was reduced to safe value  $\sim 10\text{ W/m}$

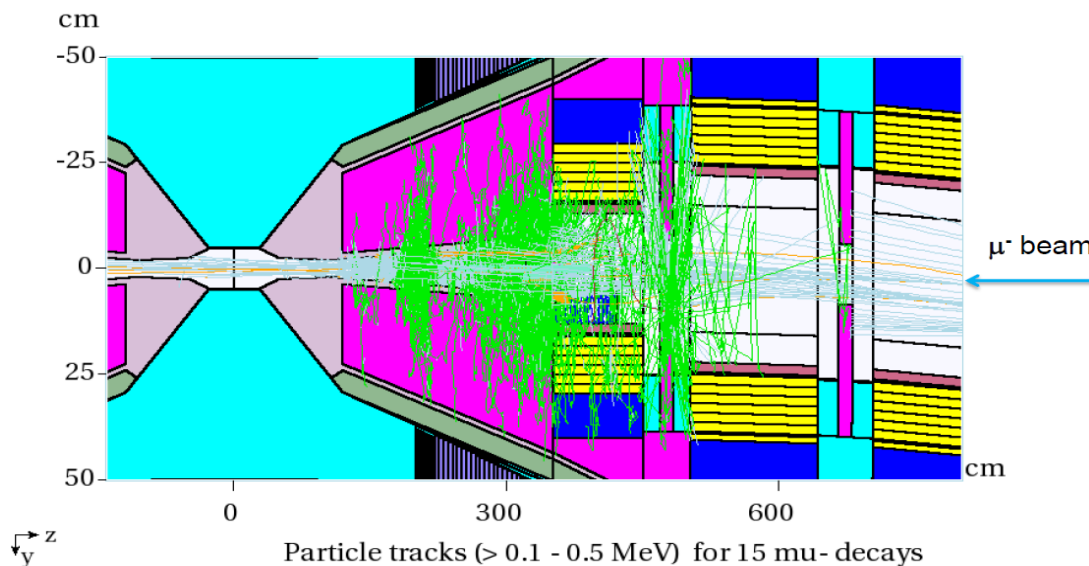




# Higgs Factory Detector Backgrounds

Expect poorer performance compared to 1.5 TeV MC:

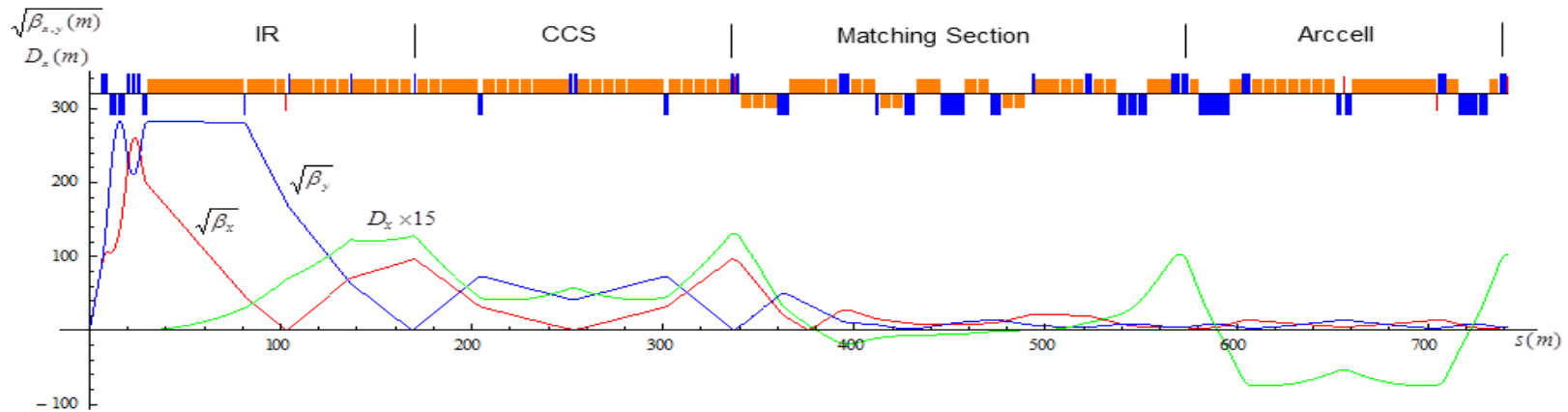
- geometrically larger aperture,
- almost twice shorter, substantially thinner cone,
- 2.5 times shorter trap and
- 3.5 longer tip-to-tip open region ( $\pm 2\sigma_z$  plus no extra shadowing for collision products)



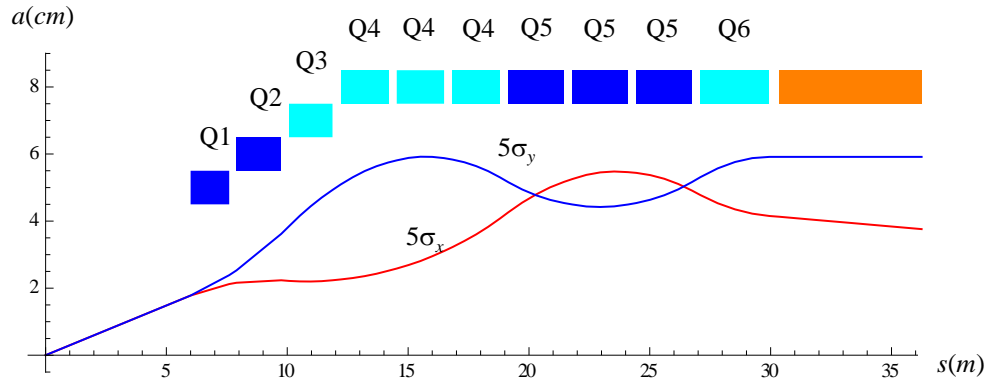
Particle		1.5-TeV MC 10deg	125-GeV HF V2 (MAP13 06/13)	125-GeV HF V7x2s4 (Jan. 2014)
Photon	<b>N</b> <b>E</b>	$1.8 \times 10^8$ 160 $\langle E \rangle = 0.9$ MeV	$3.2 \times 10^9$ 12000	$2.8 \times 10^8$ 2200 $\langle E \rangle = 8$ MeV
Electron	<b>N</b> <b>E</b>	$1.0 \times 10^6$ 5.8 $\langle E \rangle = 6$ MeV	$1.2 \times 10^8$ 9000	$2.0 \times 10^6$ 32 $\langle E \rangle = 16$ MeV
Neutron	<b>N</b> <b>E</b>	$4.1 \times 10^7$ 170	$1.7 \times 10^8$ 300	$5.2 \times 10^7$ 86
Ch. Hadron	<b>N</b> <b>E</b>	$4.8 \times 10^4$ 12	$1.0 \times 10^5$ 26	$1.0 \times 10^4$ 2.3
Muon	<b>N</b> <b>E</b>	$8.0 \times 10^3$ 184 $\langle E \rangle = 23$ GeV		$2.8 \times 10^3$ 8.2 $\langle E \rangle = 3$ GeV

This number is challenged by Tom Markiewicz. Is the same shielding geometry, energy cuts etc. used?

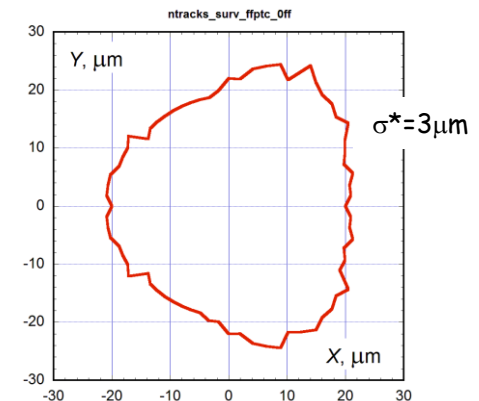
# $E_{\text{com}} = 3\text{TeV}$ Collider Lattice



Optics functions from IP to the end of the first arc cell (6 such cells / arc) for  $\beta^* = 5\text{mm}$

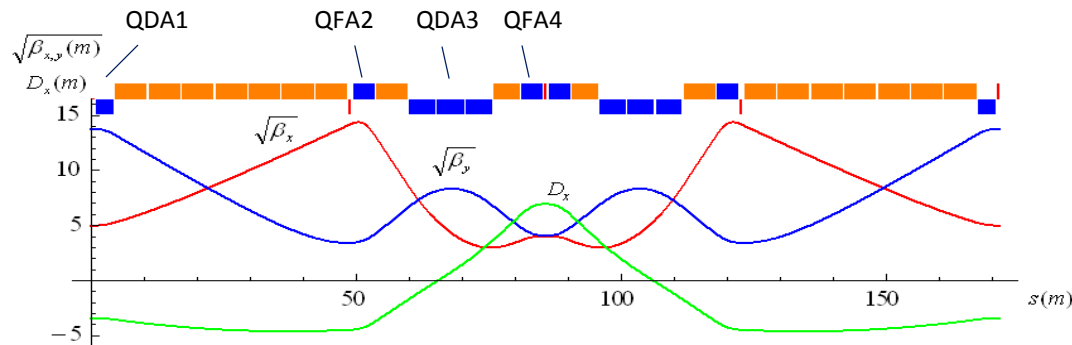


5 sigma beam sizes and magnet inner radii.  
 Q3, Q4 and Q6 have 2T dipole component.  
 $B_{\text{pole tip}} = 12\text{T}$  for shown apertures, can be reduced to 10T -  
 we do not need  $5\sigma$  for the beam scraped at  $3\sigma$ .



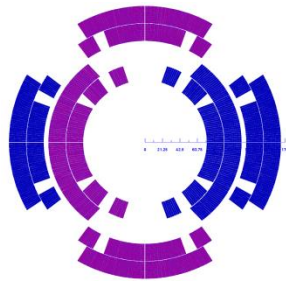
The dynamic aperture w/o field errors  
 $\approx 6\sigma$ . The stable momentum range  $\pm 0.7\%$

# Combined Function Magnets for the Arcs

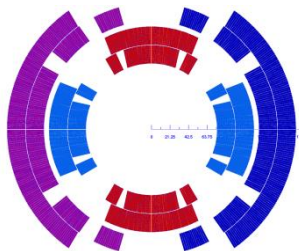


## Motivation:

- Spread decay v's
- Sweep away decay electrons before they depart from median plane - allows for azimuthally tapered absorber



Dipole/Quad



Quad/Dipole

Parameter (4.5K)	D/Q QDA1/3	Q/D	
		QDA1/3	QFA2/4
Maximum field in coil (T)	16.8/16.7*	16.5/17.5	
Maximum field or gradient in aperture (T or T/m)	9.3/76.7	12.0/72.5	
Operating field or gradient (T or T/m)	9.0/35.0	9.0/35.0	8.0/85.0
Fraction of SSL at the operating field	0.75/0.61*	0.70/0.64	0.75/0.86
Inductance $L_{self}$ (mH/m)	16.0/20.6*	44.2/6.9	
Stored energy E at the operating field (MJ/m)	1.5/0.5	2.9/0.1	2.3/0.6
Horizontal Lorentz force $F_x$ at the operating field (MN/m)	7.7/-0.1#	7.2/2.2	6.1/5.5
Vertical Lorentz force $F_y$ at the operating field (MN/m)	-4.5/-1.6	-4.0/-0.3	-4.5/-1.5
Length (m)	3.34/5.0	3.34/5.0	1.8/2.8
Aperture (mm)	150	150	150

\* the first value is for dipole coils, the second one is for quadrupole coils;

# totals per quadrant in dipole and per octant in quadrupole.

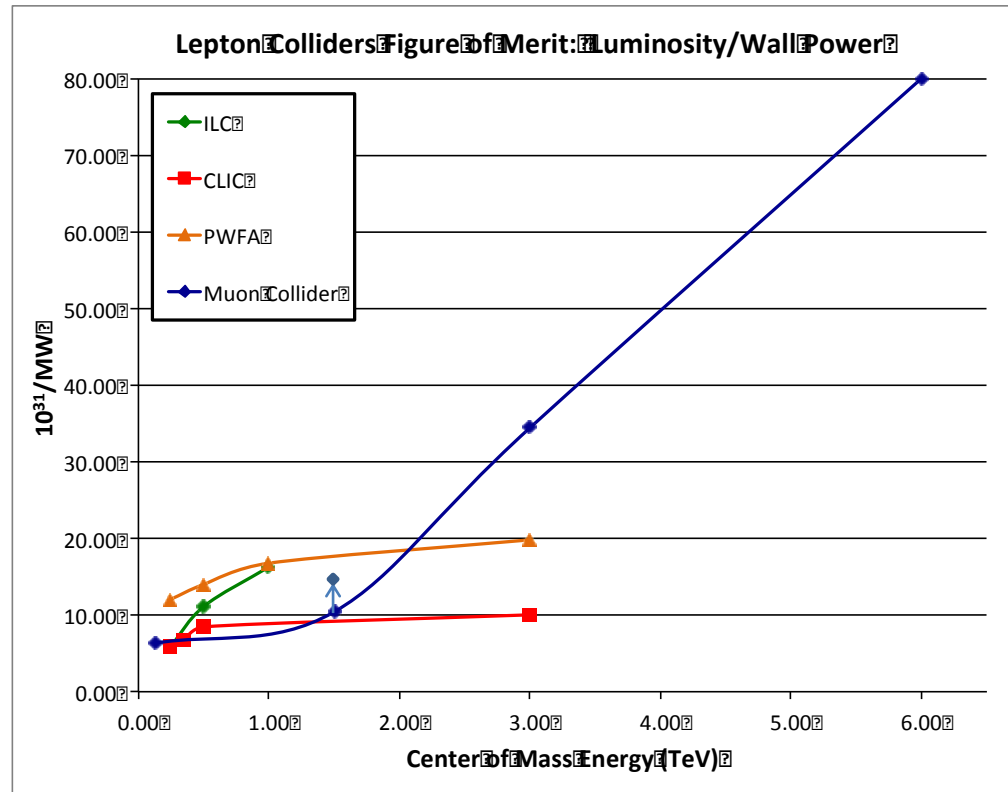
- Quad/Dipole design appears superior
- Preliminary analysis shows heat deposition in coils < 1.5 mW/g with only 2cm thick absorbers. However a thicker absorber can be required to keep the heat load below 10W/m

# Design Parameters

Muon Collider parameters				
Collision energy, TeV	0.126	1.5	3.0	6.0*
Repetition rate, Hz	30	15	12	6
Average luminosity / IP, $10^{34}/\text{cm}^2/\text{s}$	0.0025	1.25	4.6	13
Number of IPs	1	2	2	2
Circumference, km	0.3	2.5	4.34	6
$\beta^*$ , cm	2.5	1	0.5	0.25
Momentum compaction factor	0.08	$-1.3 \cdot 10^{-5}$	$-0.9 \cdot 10^{-5}$	$-0.5 \cdot 10^{-5}$
Normalized emittance, $\pi \cdot \text{mm} \cdot \text{mrad}$	300	25	25	25
Momentum spread, %	0.003	0.1	0.1	0.1
Bunch length, cm	5.6	1	0.5	0.25
Number of muons / bunch, $10^{12}$	2	2	2	2
Number of bunches / beam	1	1	1	1
Beam-beam parameter / IP	0.007	0.09	0.09	0.09
RF frequency, GHz	0.2	1.3	1.3	1.3
RF voltage, MV	0.1	12	85	530
Proton driver power (MW)	4	4	4	2

First attempt made by M.-H. Wang (SLAC), requires stronger magnets to keep  $L \sim E^2$

# Luminosity / Wall Power Comparison



1.5 TeV design used doublet FF, with quadruplet FF  $\beta^*$  can be made smaller and luminosity ~50% higher

## Design Status

$E_{\text{com}}$ (TeV)	Lattice design	Magnet design	Heat deposit.	MDI design	Magnet error corr.	Beam-beam & coherent
0.126	✓	✓	✓	✓	✓	✓
1.5	✓	✓	✓	✓	✓	✓
3.0	✓	✓	✓	—	—	—
6.0	—	—	—	—	—	—

### If work on the Muon Collider will be resumed:

- Finish the 3TeV MC design (improve  $\beta^*$ -tuning section, design MDI, address beam collimation/halo extraction problem)
- Study tolerances on random field errors and misalignments - of general importance for understanding the real constraints on beta-functions, momentum compaction factor etc.
- Try larger dipole component in IR quads to reduce backgrounds
- Develop cryostat concept integrated with W absorbers and masks
- Start 6TeV lattice - with stronger HTS + LTS magnets (?)
- Re-design 1.5 TeV MC with quadruplet FF - if there is physics within its reach

# Very High-Energy MC Prospects

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Higher magnetic fields (and gradients) are the key to high luminosity:

- Circumference
- $\beta^*$

From A. Zlobin's talk at the previous MAP meeting:

Higher field magnets – *outside of the MAP scope and resources => GARD*

15 T Nb<sub>3</sub>Sn magnets with coil ID~20(40) cm, B<sub>des</sub>~18 T – *new class of Nb<sub>3</sub>Sn accelerator magnets*

20 T HTS/LTS magnets (10 T HTS insert) with ~20 cm bore,

B<sub>des</sub>>25 T – *new magnet technology*

*significant R&D effort is needed!!!*

But we need now an educated guess of what will be feasible within 20 years

# Achievements

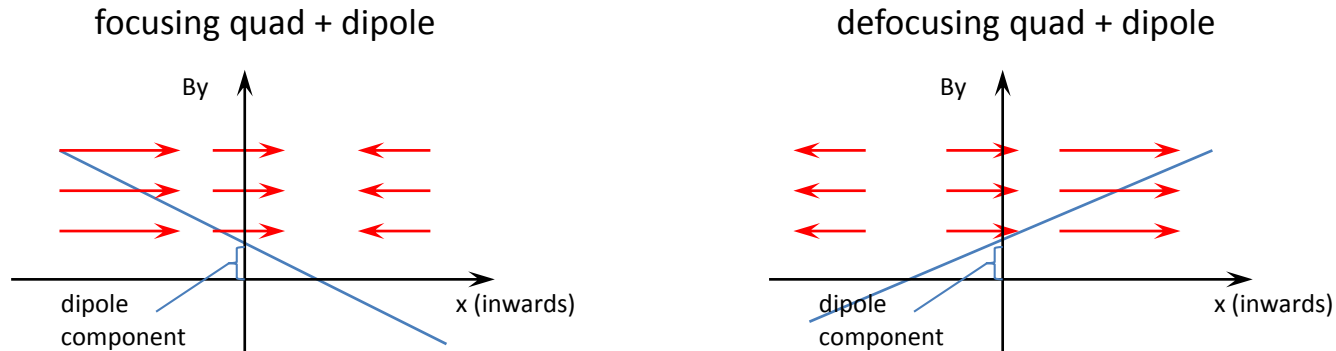
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## Concepts developed in the course of work on HF, 1.5TeV and 3TeV MC:

- 3-sextupole chromaticity correction scheme
- Quadruplet Final Focus (not implemented in the chronologically first 1.5TeV design)
- New Flexible Momentum Compaction arccell design (High Energy MC)
- $\beta^*$ -tuning section with a chicane (for  $E_{\text{com}} \geq 3\text{TeV}$ )
  
- Dipole component in IR quad is proven to reduce backgrounds
- Nozzle, cone, masks optimization Backgrounds in 1.5TeV MC (and in HF?) on par with LHC
- Classical cos-theta dipole with inner absorbers found superior to open-midplane
- Magnet studies for 0.125, 1.5 and 3 TeV MC are almost complete, apertures as large as 0.5m do not pose a problem
- Optimum configuration for combine-function magnets - a nested Quadrupole/Dipole magnet - found



## Support slide - Why Quadruplet Final Focus?



- Dipole component in a defocusing quad is more efficient for cleaning purposes – it is beneficial to have the 2<sup>nd</sup> from IP quad defocusing
- The last quad of the FF “telescope” also must be defocusing to limit the dispersion “invariant” generated by the subsequent dipole (not shown)

$$J_x = \frac{D_x^2 + (\beta_x D'_x + \alpha_x D_x)^2}{\beta_x} \approx \beta_x \phi^2$$

– both requirement are met with either doublet or quadrupole FF:

